

The collisional formation of massive stars

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Model of Bonnell, Bate & Zinnecker 1998 (BBZ)

proposed because:

- A) theoretical difficulties with accretion due to p_{rad} (Wolfire & Casinelli 1989; but see Edgar & Clarke 2003, Sonnhalter & Yorke 2002)
- B) lack of observed discs in massive protostellar cores but see Cesaroni et al 2006 (PPV) et seq.

BUT: ARE THERE (EXOTIC?) ENVIRONMENTS WHERE COLLISIONS ARE EVER IMPORTANT?

Required densities for stellar collisions on Myr timescale is high ($\sim 10^8 / \text{pc}^3$)

Stolte et al 2006

Cluster	M_{total} (M_{\odot})	Extent (pc)	r_{core} (pc)	ρ_{core} ($M_{\odot} \text{pc}^{-3}$)	Age (Myr)
Arches	10^4	1 (?)	0.2	3×10^5	2–3
NGC 3603 YC.....	$>7 \times 10^3$	4.4	0.2	10^5	1–3
R136.....	2×10^4	4.7	0.02	5×10^4	1–5
Orion.....	10^3	3	0.2	4×10^4	0.3–1
Antennae starbursts.....	10^4 – 10^6	1–10	?	10^3	1–20
Milky Way GCs.....	10^4 –few 10^5	Few pc	≈ 1	10^2 – 10^6	10 Gyr

...collisions unimportant for observed clusters in their current states....

Elements of (BBZ) model:

(spherical, non-rotating gas, all gas onto stars)

i.e. $\dot{t}_M \gg t_{\text{dyn}}$

Adiabatic accretion onto star cluster results
in shrinkage:

$$r \propto M^{-3}$$

Can understand in terms of preservation of
adiabatic invariant (e.g. angular
momentum)

Or revirialisation after accretion of gas with

Model scalings

- $R \sim M^{-3}$

Don't need to accrete much mass to ensure density rises

DRAMATICALLY

- $N \sim M^9$

- $\rho \sim M^{10}$

- $V \sim M^2$

Velocity dispersion increases more mildly (\Rightarrow encounters remain in grav focused regime)

Model limitations

- Adiabatic regime requires $\dot{M} < v^3/G$ (for v = initial velocity cluster vel. dispersion)
- More amply satisfied during collapse (once adiabatic => always adiabatic)
- If cluster fed by gas free-falling from outer cluster/reservoir, adiabatic condition implies v for cluster $> v$ for reservoir

End state

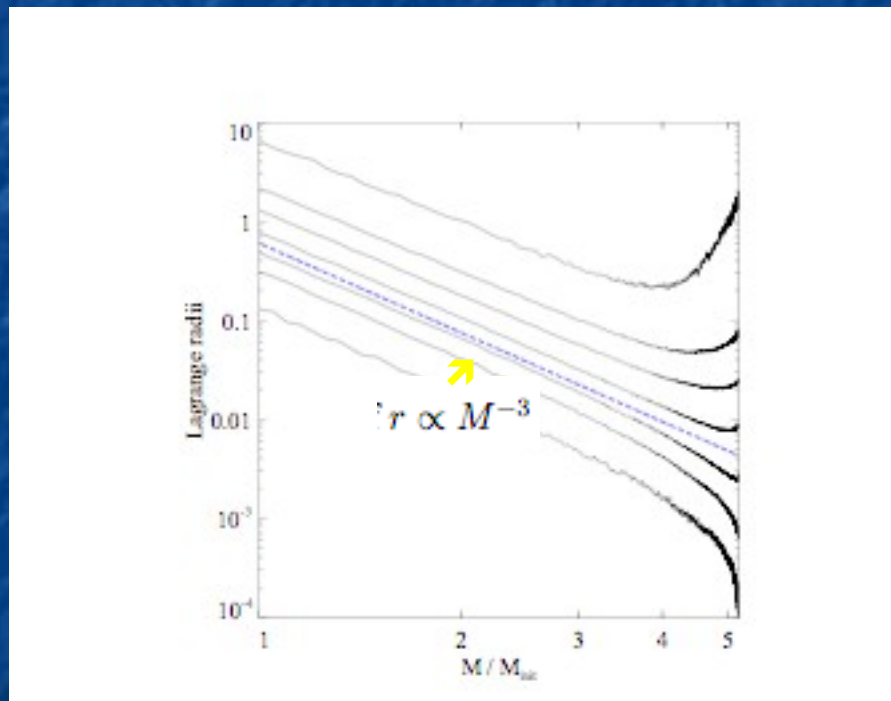
- If adiabatic regime persists `forever' are collisions inevitable if keep on accreting?
- Bonnell & Bate 2002 found "no" - needed to boost collision cross-section to get collisions before clusters puff up due to few body effects
- => Clarke & Bonnell (2008) argued that collisions require large N, massive clusters (not ONC!)

Follow up with Monte Carlo code (Freitag & Benz 2001,2002)

- Models of spherical clusters in dynamical equilibrium
 - Include secular effects:
 - a) accretion
 - b) two-body relaxation
 - Estimate collision rate through post-processing
- Equal mass stars !

Results

End of adiabatic regime



← Puffing up

← Core collapse!

End of adiabatic regime when

$$t_{2r} \sim t_{\dot{M}} (= M/\dot{M})$$

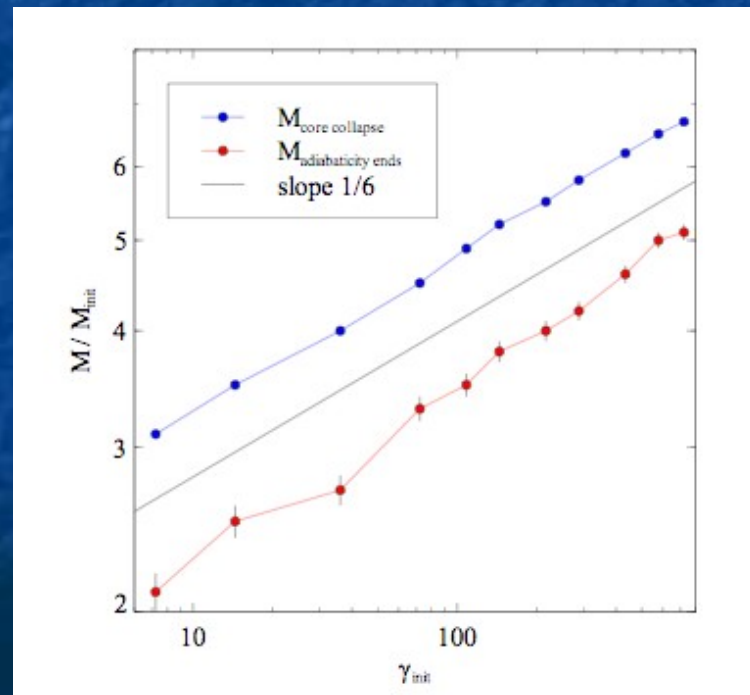
Ratio of $t_{2r}/t_{\dot{M}}$ (initially large) scales as M^{-6}



$$M_f \propto \gamma_{init}^{\frac{1}{6}}$$

Where

$$\gamma \equiv \frac{t_{2r}}{t_{\dot{M}}}$$

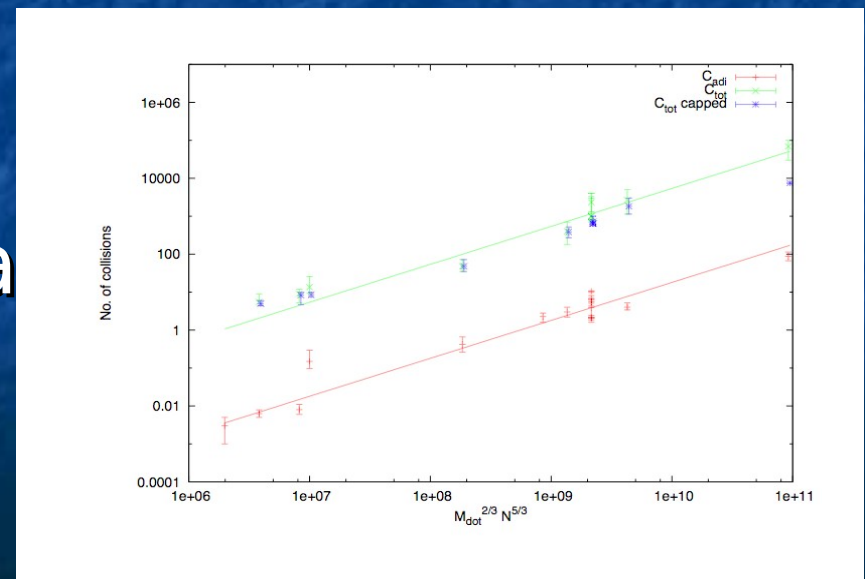


Estimate number of collisions in adiabatic phase (collapse homologous)

- Number of collisions per mass doubling time scales as M^{-10} during collapse so can relate total collisions to number collisions in first mass doubling time and

$$\gamma \equiv \frac{t_{2r}}{t_M} \quad (\text{since } M_f \propto \gamma^{\frac{1}{6}})$$

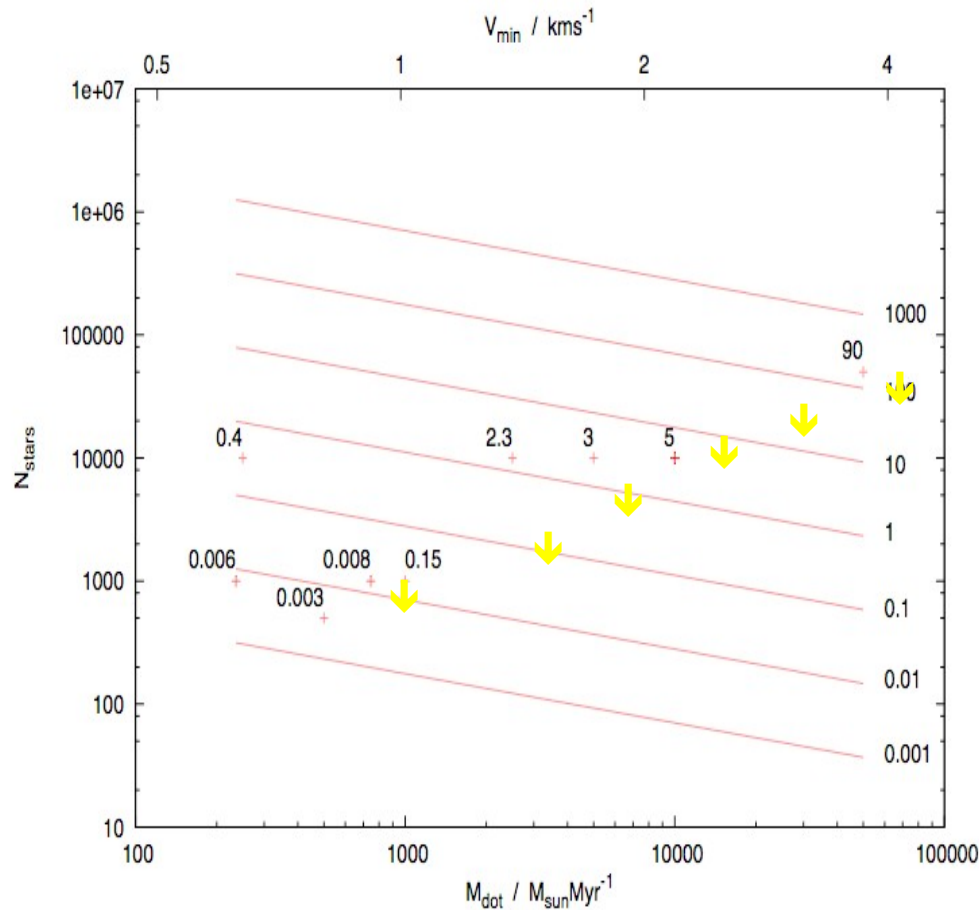
find C_{adi} proportional to $N^{5/3} \dot{M}^{2/3}$



Numerical values (red contours = number of collisions in adiabatic regime)

Minimum initial velocity as function of

\dot{M} s.t. enter adiabatic collapse



Have to be
below arrows to
drive collapse in
a Myr

⇒ NEED VERY

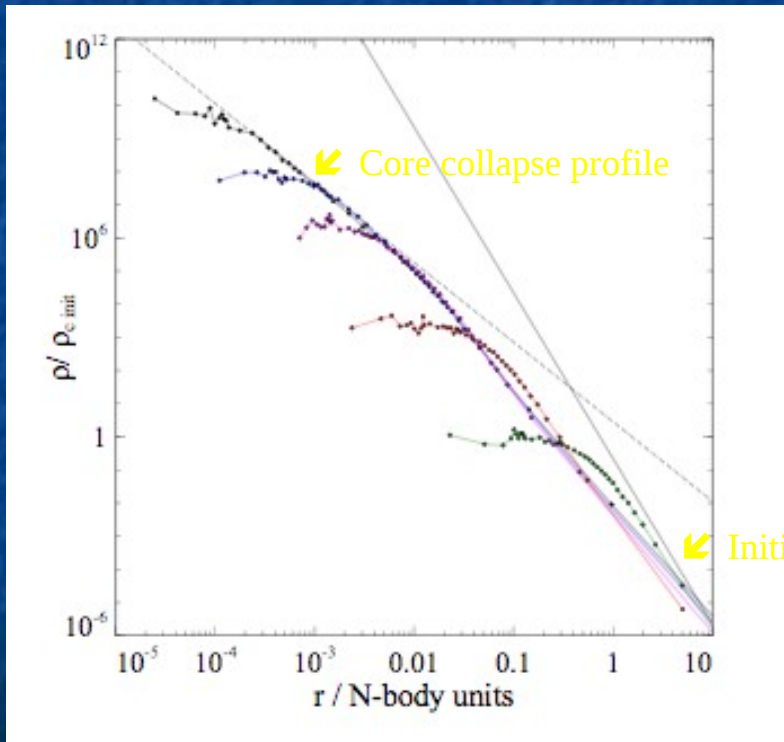
HIGH N ($\sim 10^4$

- 10^5) TO GET

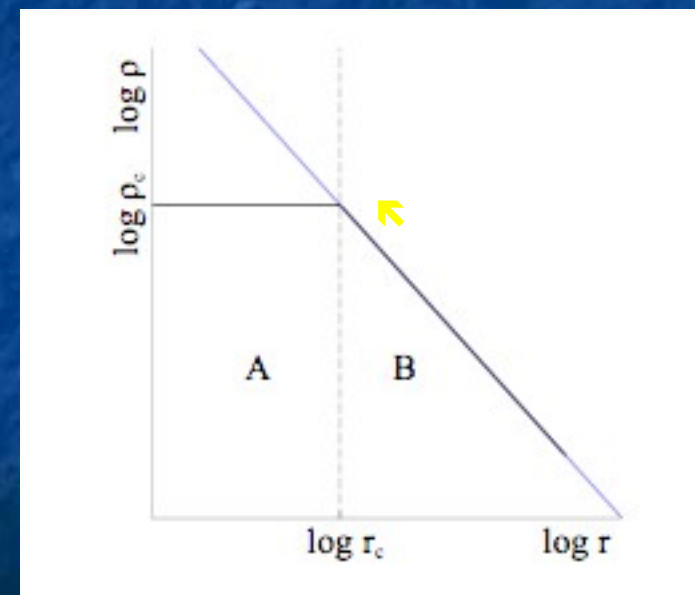
EVEN A FEW

COLLISIONS

But adiabatic regime is not the end of the story - also examine collisions during core collapse



Schematic of density evolution during core collapse



Collisions predominantly from $\sim r_c$

As approach core collapse, system evolves on \sim core relaxation time

Time to core collapse

$$\tau = t_{2r}/\eta_c$$

Evolution of core radius

$$r_c \propto (\tau\eta)^{5/9}$$

Evolution of collision rate

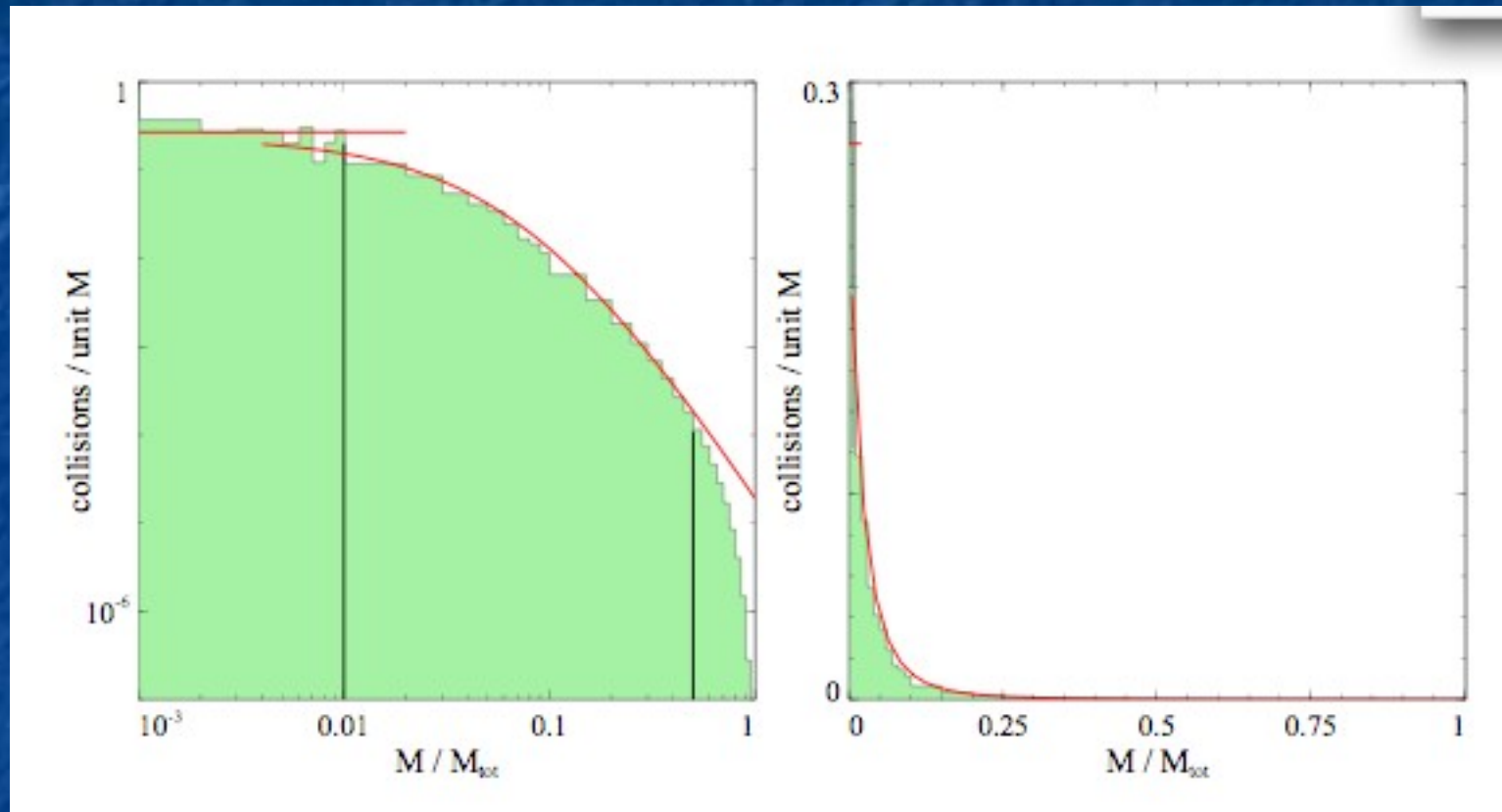
$$\dot{C}_{tot} \propto r_c^{-1.6}$$

$$\dot{C} \propto (\tau\eta)^{8/9}$$

=>

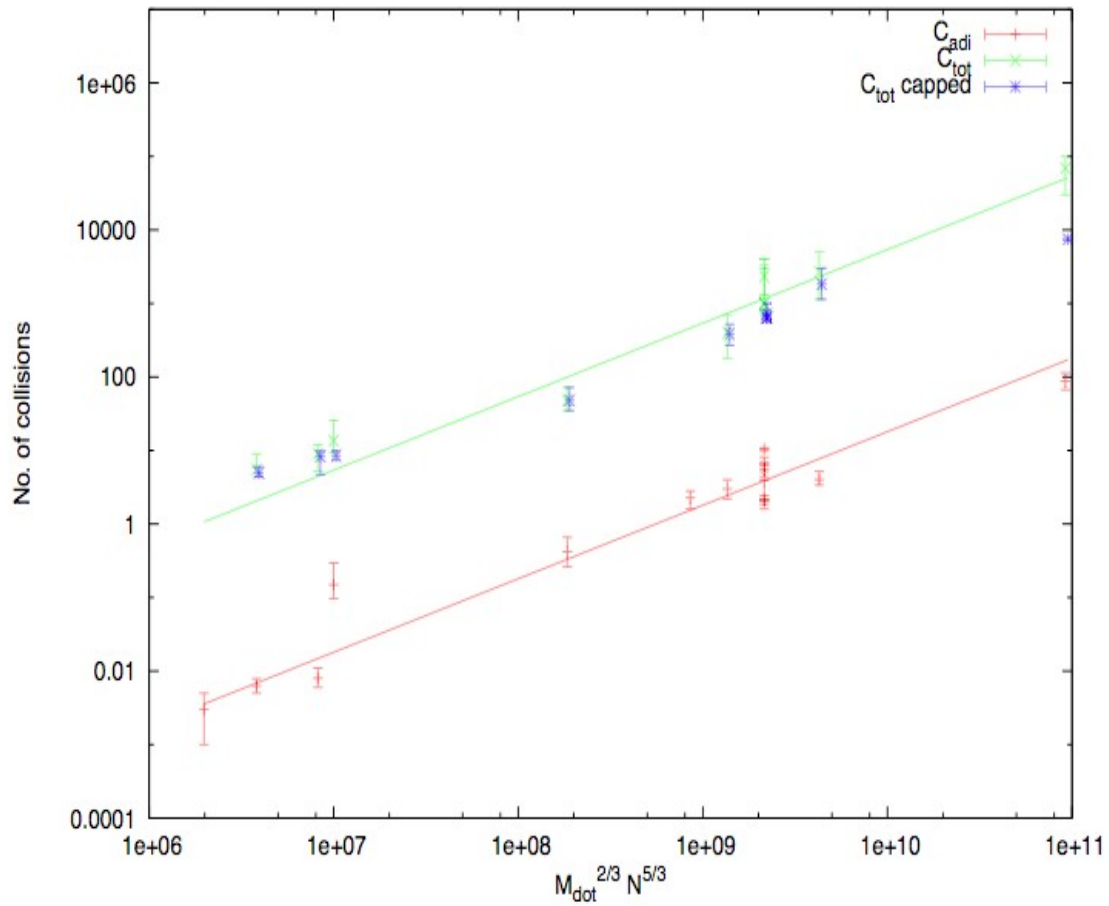
total number of collisions converges

Where the collisions occur



Mostly within innermost 10%
of mass

Factor 30!



← Collisions

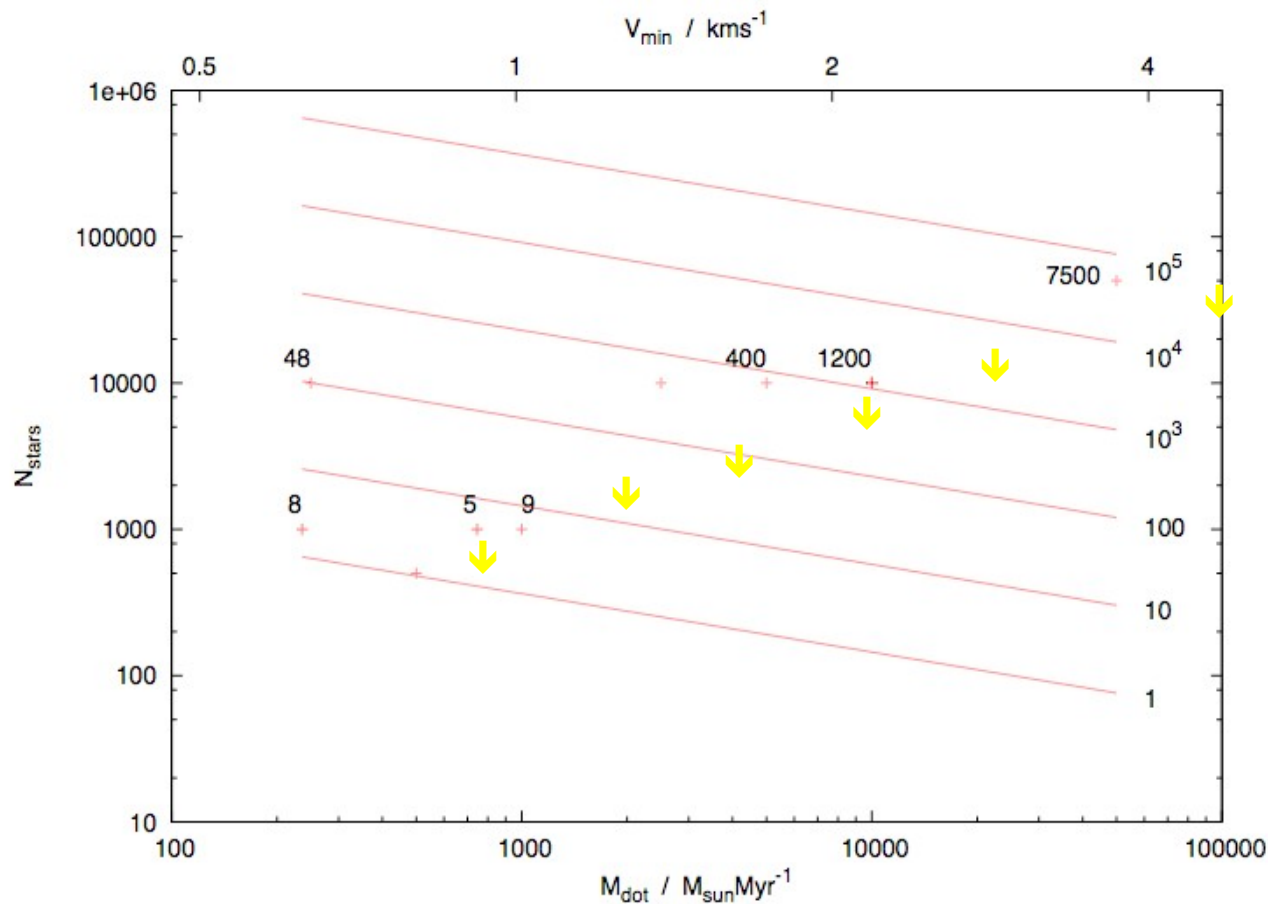
during core

collapse
← Collisions

in adiabatic

regime

Red contours denote number of collisions in core collapse regime



← Interesting number
of collisions in core
collapse regime in
populous clusters

But would binaries prevent core collapse?

- Three-body binaries only effective in small N clusters
- Primordial binaries? Maybe, but need substantial population of sub-AU binaries

Conclusion

- Don't expect many collisions in adiabatic regime even in large N , massive clusters
- But collision yield rises by ~ 30 if core collapse goes to completion- now astronomically interesting in large N , massive systems

Do you get latter phase in realistic case (primordial binaries + mass spectrum)?

Adding the realism:

- . Include mass spectrum in Monte Carlo (large N) simulations
- . Nbody + accretion calculations to include binaries (Nbody6 + “negative stellar winds”)