# 2D models of layered protoplanetary discs

(R. Wünsch, H. Klahr, M. Różyczka, A. Gawryszczak)

R. Wünsch, H. Klahr and M. Różyczka, 2005, MNRAS, 362, 361 The ring instability

R. Wünsch, A. Gawryszczak, H. Klahr and M. Różyczka, 2005, MNRAS, submitted The effect of a residual viscosity in the dead zone

### The fate of late planets

(R. P. Nelson, R. Wünsch, M. Różyczka)

# Layered-disc: basic idea (Gammie, 1996)



- MRI does not operate in regions with low ionization dead zone
- ionization sources: particle collisions (T > 1000K), cosmic rays & X-rays (surface layers  $\sim 100 \text{ g cm}^{-2}$ )
- disc structure: IAR, LAR (=  $2 \times ASL$  + DZ), OAR
- in LAR:  $\dot{M} = \dot{M}(r) \Rightarrow$  mass accumulation in the dead zone

$$\dot{\Sigma}_{\mathrm{DZ}} = \frac{1}{2\pi r} \frac{\partial M}{\partial r}$$

# **Numerical model**

- based on RHD code TRAMP: (Klahr et al., 1999)
- radiation transfer: flux limited diffusion approximation
- 2D axially symmetric in spherical  $(r, \theta)$  coords.



# **Ring instability - mechanism**

• dead zone decomposes into rings

#### ring instability mechanism:

- thickness of surface layer H<sub>a</sub> depends on the dead zone thickness H<sub>DZ</sub> (due to different vertical gravity)
- $\blacktriangleright\ \dot{M}$  depends on derivative of  $\nu$   $\Rightarrow$  it is smaller in inner edge and higher in outer edge of the ring
- $\triangleright$  enhanced mass accumulation in the ring  $\Rightarrow$  positive feedback





- rings may work as traps for the dust  $\rightarrow$  formation of planets
- rings may decay due to the hydrodynamic instability, if  $q > \sqrt{3}$  $(\Omega \sim r^{-q})$

(Papaloizou & Pringle, 1985)

# **Ring instability - influence of irradiation**

analytical approximative approach:  $T_i^4 = \frac{3}{8}\tau T_e^4 + WT_\star^4$ 

- changes the vertical structure of the unperturbed disc
  - ▷ conical disc:  $W = \frac{2}{3\pi} \left(\frac{R_{\star}}{r}\right)^3 \rightarrow$  viscous term always dominates
  - ▶ flaring disc:  $W = \alpha_{\rm gr} \left(\frac{R_{\star}}{r}\right)^2$ , for  $H/r \sim r^{2/7}$ → irradiation important for r > 10 AU

#### ullet smoothes the temperature $\Rightarrow$ suppresses the ring instability

▷ grazing angle of the inner edge of the ring:  $\alpha_{gr} \sim \frac{\delta_k}{l(\delta_0 + \delta_k)} + \frac{2}{3\pi} \frac{R_{\star}}{r}$  $\rightarrow \nu(\delta_k, \delta_0, r, l)$ 



perturbation of the disc thickness has to reach a certain value, then the instability can grow



# Viscosity in the dead zone - motivation

- indications for a small viscosity in the dead zone  $\rightarrow$  the undead zone
- caused by purely hydrodynamic turbulence excited by waves propagating from MRI-active surface layers (Fleming & Stone, 2003)
- viscosity in DZ  $\sim 10\%$  viscosity in active parts Our models
- models with different  $\nu$  computed for several 1000 orb.:
  - ▶ definition of  $\nu$ :  $\nu = \alpha c_s H_a$  vs.  $\nu = \alpha c_s^2 / \Omega$
  - $\triangleright$  viscosity in active parts  $\alpha_a = 0.005, 0.01, 0.02$
  - $\triangleright$  viscosity in the dead zone  $\alpha_{DZ} = 0, 0.01$  and  $0.1\alpha_a$

# **Results - minioutbursts**



- $\alpha_{\rm DZ} = 0, 0.01 \alpha_a \rightarrow \text{rings},$  $\alpha_{\rm DZ} = 0.1 \alpha_a \rightarrow \text{mini-outbursts}$
- high viscosity ( $\alpha_a = 0.02$ )  $\rightarrow$  regular narrow mini-outbursts, outer part of DZ stationary





# **Layered disc with** $\alpha_{DZ} \neq 0$

- analytical description of layered disc with  $\alpha_{DZ} \neq 0$ :  $\dot{M} = 12\pi r^{1/2} \frac{\partial r}{\partial} (\nu_a \Sigma_a + \nu_{DZ} \Sigma_{DZ}), \qquad T_m^4 = \frac{3}{8} \kappa T_e^4 \frac{\alpha_a \Sigma_a^2 + \alpha_{DZ} \Sigma_{DZ} (\Sigma_{DZ} + 2\Sigma_a)}{\alpha_a \Sigma_a + \alpha_{DZ} \Sigma_{DZ}}$   $T_e^4 = \frac{9}{4\sigma} \Omega^2 (\nu_a \Sigma_a + \nu_{DZ} \Sigma_{DZ})$
- mid-plane temperature  $T_m$  depends on the surface density  $\Sigma = 2(\Sigma_a + \Sigma_{\rm DZ})$  (contrary to LD with  $\alpha_{\rm DZ} = 0$ )
- ignition surface density

$$\Sigma_{\rm ign} = 2 \left( \frac{320\sigma}{27} \frac{\mu m_{\rm H}}{k_{\rm B} \Omega \alpha_{\rm DZ}} T_{\rm lim}^{5/2} - \frac{\alpha_a - \alpha_{\rm DZ}}{\alpha_{\rm DZ}} \Sigma_a^2 \right)^{1/2}$$

• surface density necessary to maintain the disc active

$$\Sigma_{\rm mtn} = \left(\frac{1280\sigma\mu m_{\rm H}}{27k_{\rm B}\alpha_a\Omega}\right)^{1/2} T_{\rm lim}^{5/4}$$

#### Mini-outbursts - mechanism



#### **Evolution of one outburst**



# **Stationary states**

- we search for stationary surface density profiles using 1D code similar to Stepinski (1999) or Armitage et al. (2001)
- numerically solve equation  $\dot{\Sigma} = \frac{1}{2\pi r} \frac{\partial \dot{M}}{\partial r}$
- determines  $T_m$  from  $\Sigma$ , decides if LD or  $\alpha$ D, computes M, advects mass between cells
  - $\triangleright$  stationary solution exist above  $R_1$
  - part of DZ between R<sub>1</sub> and R<sub>2</sub> can be ignited externally
  - it contains mass

$$\begin{array}{l} 2.0 \times 10^{-7} \mathrm{M}_{\odot} \text{ for } \dot{M} = 10^{-8} \ \mathrm{M}_{\odot} \, \mathrm{yr}^{-1} \\ 2.7 \times 10^{-4} \mathrm{M}_{\odot} \text{ for } \dot{M} = 10^{-7} \ \mathrm{M}_{\odot} \, \mathrm{yr}^{-1} \\ 0.01 \mathrm{M}_{\odot} \text{ for } \dot{M} = 10^{-6} \ \mathrm{M}_{\odot} \, \mathrm{yr}^{-1} \end{array}$$



### **Conclusions**

- no (or very small) viscosity in DZ  $\Rightarrow$  ring instability
- $\alpha_{\rm DZ} \neq 0 \Rightarrow$  the oscillations of the inner edge of DZ
- stationary accretion ( $\dot{M} = {\rm const}$ ) at higher radii; DZ consists of 3 parts: oscillating, stationary combustible, and stationary incombustible

### **Conclusions**

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#### Future

- going to 3D (to see what happens with rings and minioutbursts without the assumption of spherical symmetry)
- irradiation by the central star
- more complicated ionization structure (ionization by X-rays,
  - ...)

- 2d vertically averaged locally isothermal model of the disc (NIRVANA/FARGO code)
- disc is very light ( $\sim 1 M_J$  within 12.5 AU), and viscous ( $\alpha = 0.01 0.05$ )
- planet of  $\sim 30 M_\oplus$  migrating, accreting mass



 the aim is to determine how far the planet migrates and how much mass it accretes

### **First results**

- planet radius drops by several percent (2-3)
- planet accretes mass  $0.4-0.6 M_{\rm J}$





- technical problems: unphysical outwards migration occurs
- related to the poor resolution of the accretion region
- antialiasing seems to help

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